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Digitally Tunable MDAC-Based State Variable Filter Reference Design



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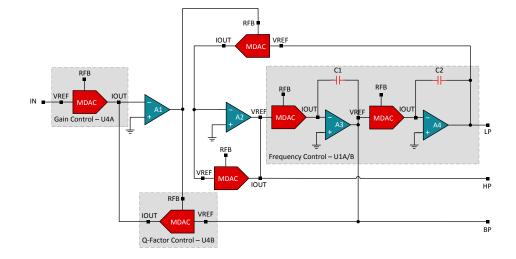
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Circuit Description

This MDAC based state variable filter offers highly accurate digital tuning of gain, center/cut off frequency, and quality factor. This circuit provides three separate filter outputs: low pass, band pass, and high pass that can be accessed simultaneously.



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1 Design Summary

The design requirements are as follows:

Supply Voltage: 5 V

AC Input: 1 V_{PP}

Output: Low pass, Band pass, High pass

Tunability: Gain, Center/Cut off Frequency, and Quality Factor

The design goals and performance are summarized in Table 1. Figure 1 depicts the measured transfer function of the design.

Table 1. Comparison of Design Goals, Simulation, and Measured Performance

| | Goal | Simulated | Measured |
|----------------------|----------------------------------|----------------------|----------------------|
| Cut Off Frequency | 10 Hz to 30kHz | 2.11 Hz to 27.98 kHz | 1.99 Hz to 28.76 kHz |
| Range (3dB) | DAC Code Range: 0x0004 to 0xFFFF | | |
| Coin Donne | 0 dB to 6dB | -54.13 dB to 6.02 dB | -53.31 dB to 6.01 dB |
| Gain Range | DAC Code Range: 0x0040 to 0xFFFF | | |
| Quality Factor Range | 0 dB to 6dB | 0.47 to 2.15 | 0.46 to 2.14 |
| Quality Factor Range | DAC Code Range: 0xFFFF to 0x4000 | | |

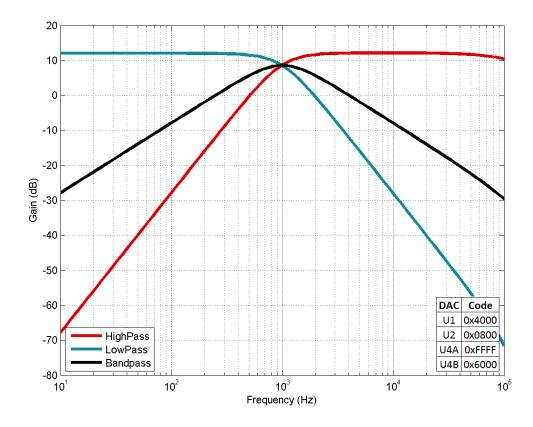


Figure 1: Measured Transfer Function



2 Theory of Operation

An implementation of a state variable filter using discrete resistors is shown in Figure 2

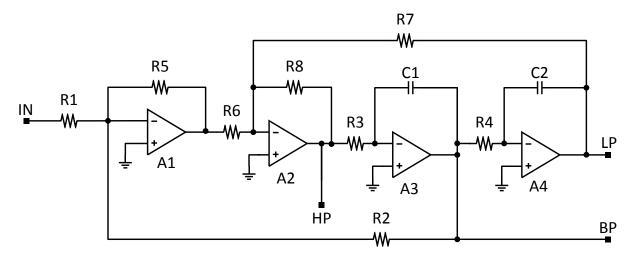


Figure 2: State Variable Filter

In Figure 2, amplifier A1 and A2 form summing and inverting stages followed by two op amp integrators, A3 and A4 which act as single pole low pass filters. Amplifiers A3 and A4 are cascaded to form a second-order filter. This configuration provides 3 filter outputs: low pass (LP), band pass (BP) and high pass (HP). The center frequency (in the case of the band pass) or cut off frequency (in the case of the high pass and low pass) is set by theRC circuits on both integrators. For simplicity, this RC combination is typically made equal i.e. R3 = R4 and C1 = C2.

In order to analyze this circuit, nodal equations for each node in the circuit must be solved. The resulting transfer function is shown in Equations 1, 2 & 3.

$$\frac{LP}{IN} = \frac{\frac{R_5 \cdot R_8}{C_1 \cdot C_2 \cdot R_1 \cdot R_3 \cdot R_4 \cdot R_6}}{s^2 + \frac{R_5 \cdot R_8}{C_1 \cdot R_2 \cdot R_3 \cdot R_6} \cdot s + \frac{R_8}{C_1 \cdot C_2 \cdot R_3 \cdot R_4 \cdot R_7}} \tag{1}$$

$$\frac{BP}{IN} = \frac{-\frac{R_5 \cdot R_8}{C_1 \cdot R_1 \cdot R_3 \cdot R_6} \cdot s}{s^2 + \frac{R_5 \cdot R_8}{C_1 \cdot R_2 \cdot R_3 \cdot R_6} \cdot s + \frac{R_8}{C_1 \cdot C_2 \cdot R_3 \cdot R_4 \cdot R_7}}$$
(2)

$$\frac{HP}{IN} = \frac{\frac{R_5 \cdot R_8}{C_1 \cdot R_1 \cdot R_3 \cdot R_6} \cdot s^2}{s^2 + \frac{R_5 \cdot R_8}{C_1 \cdot R_2 \cdot R_3 \cdot R_6} \cdot s + \frac{R_8}{C_1 \cdot C_2 \cdot R_3 \cdot R_4 \cdot R_7}}$$
(3)

$$C_1 = C_2$$
, $R_3 = R_4$, $R_7 = R_8$ (4)



Equations 1, 2 & 3 are simplified by making the assumptions in Equation 4. Comparing the resulting equations with the standard equation for a band pass filter (Equation 5), yields expressions for gain (A_0) , center/cut off frequency (ω) , and quality factor (Q) (Equations 6, 7 & 8).

$$\frac{BP}{IN} = \frac{-\frac{A_0 \cdot \omega}{Q} \cdot s}{s^2 + \frac{\omega}{Q} \cdot s + \omega^2}$$
 (5)

$$A_0 = \frac{-R_2}{R_1} \tag{6}$$

$$\omega = \frac{1}{C_1 \cdot R_3} \tag{7}$$

$$Q = \frac{R_2 \cdot R_6}{R_5 \cdot R_8} \tag{8}$$

3 Component Selection

3.1 DAC Selection

To realize eight discrete resistors a minimum of six MDACs ladders must be used. By using three dual channel MDACs with only six MDAC ladders, resistors R5 and R7 are realized by using the fixed values of two MDAC feedback resistors.

The DAC8812 is a great option for this design. It is a dual channel MDAC with strong linearity and large multiplying bandwidth which makes it ideal for this application.

Generally, MDACs are used in high performance applications that take full advantage of their strong dc specifications. MDACs have a current output and are used in conjunction with an external I-V operational amplifier. However, this design leverages the unique software-controlled output impedance property of MDACs. An important property of MDACs for this application is their reference multiplying bandwidth. The reference multiplying bandwidth changes with the programed DAC code and the bandwidth is decreased at lower codes when the reference input is highly attenuated as shown in Figure 3. Plots such as these can be found in the datasheet of any MDAC.

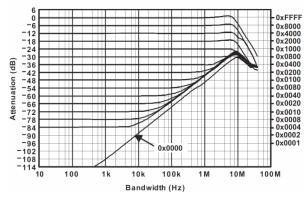


Figure 3: DAC8812 Reference multiplying bandwidth

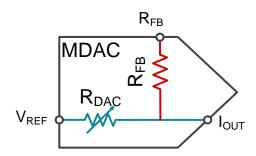


Figure 4: MDAC equivalent circuit

The resistors in Figure 2 are replaced by MDACs. The circuit equivalents of an MDAC are shown in Figure 4. Resistor R5 and R7 are realized using feedback resistors integrated in the multiplying DACs. The values of these resistors are fixed and cannot be changed by writing to the MDAC. The remaining resistors are realized by the programmable ladder impedance of the MDAC. Table 2 shows the maximum and minimum values for the tunable resistors. Note that resistors R3/R4 and resistors R7/R8 are implemented such that their values are tuned simultaneously (refer to Equation 4). To realize all the resistors in this filter a minimum of six MDACs are required. Therefore three DAC8812, a 16-Bit, dual channel serial input multiplying DAC, are used in this design. The tunable resistor range for the DAC8812 is shown in Table 2. Keep in mind that the resistor ladders in the DAC8812 can vary by ±20 percent.

| Resistors | MDAC | Minimum Value (0xFFFF Code) | Maximum Value (0x0001 Code) |
|-----------|----------|-----------------------------|--------------------------------|
| R1 | U4 A | 5.02 kΩ | 33.00 kΩ |
| R2 | U4 B | 5.02 kΩ | 25.57 kΩ |
| R3 | U2 A | 5.00 kΩ | 26.91 kΩ |
| R4 | U2 B | 5.00 kΩ | 22.86 kΩ |
| R5 | U4 B RFB | 5.18 kΩ | 5.18 kΩ |
| R6 | U1 B RFB | 4.96 kΩ | 4.96 kΩ |
| R7 | U1 B | 4.81 kΩ | 22.55 kΩ |
| R8 | U1 A | 4.81 kΩ | 22.48 kΩ |

Table 2. Measured resistor values tunable range with MDAC DAC8812

3.2 Amplifier Selection

This design requires four operational amplifiers. For all of these amplifiers, low input bias current is desired so that the critical parameters of the filter have exclusive tunability via the MDAC based resistors and their matching. The center/cut off frequency range for this design ranges from dc to 30 kHz, therefore high speed/high unity gain bandwidth amplifiers are not required.

The OPA277 was selected for this design because it features a sufficiently low input bias current of 1 nA.

3.3 Passive Component Selection

The high side cut off frequency is determined by the combination of capacitors C1 & C2 and the multiplying bandwidth of the MDAC with the lowest input code. The size of C1 is determined by Equation 7. The desired frequency bandwidth of the filters is 30 kHz. The DAC8812 reference input impedance is 5 k Ω paired with a 1 nF standard value for C1 will result in 32 kHz. In order to comply with Equation 4, both C1 and C2 must be the same value for the equations to be valid.



4 Simulation

The proposed circuit was simulated in TINA-TI™ using SPICE models of both the DAC8822 and OPA277. The choice of using the DAC8822 as a simulation model was based on the core similarity with the DAC8812 and the current lack of availability of a DAC8812 model. The DAC8822 and DAC8812 are very similar devices with the minor functional difference that the DAC8822 has more feedback resistor options. The simulation suite consists of an ac simulation test bench that included center/cut off frequency, gain and quality factor for high pass, low pass and band pass outputs.

Figure 5 shows the realization of the resistors in this circuit using MDAC DAC8822.

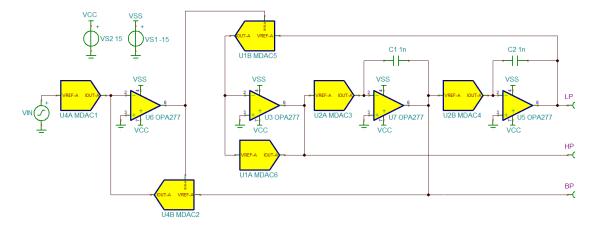


Figure 5: State Variable Filter using DAC8822

4.1 Center/Cut Off Frequency Simulation

The center/cut off frequency simulations were carried out for all the outputs (low pass, band pass and high pass). The MDAC ladders U2A/B can be tuned, thereby changing the frequency from 2.11 Hz (code 0x0004) to 27.98 kHz (code 0xFFFF). See Equation (7). Note that 0x0000 is not used in this design because at this code all the ladder switches are open and the ladder resistance is Hi-Z.

Figure 6 shows center frequency simulations for the high pass output. For frequency simulation data for band pass and low pass filters refer to Appendix B.

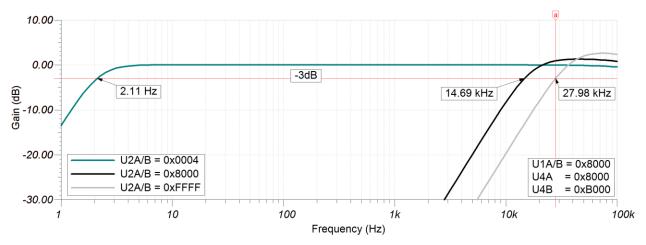


Figure 6: Cut off frequency simulation - High pass output



4.2 Gain Simulation

The gain simulations were carried out for all the outputs (low pass, band pass and high pass). The MDAC ladder U4A can be tuned, thereby changing the gain from -54.13 dB (code 0x0040) to 6.02 dB (code 0xFFFF). See Equation 6.

Figure 7 shows gain simulations for the low pass output. For gain simulation data for band pass and high pass filters refer to Appendix B.

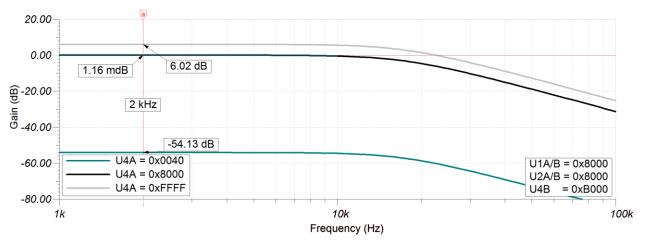


Figure 7: Gain simulation - Low pass output

4.3 Quality Factor Simulation

The quality factor simulations were carried out for all the outputs (low pass, band pass and high pass). The MDAC ladder U4B can be tuned, thereby changing the quality factor from 0.47 (code 0xFFFF) to 2.15 (code 0x4000). See Equation (8).

Figure 8 shows gain simulations for the band pass output.

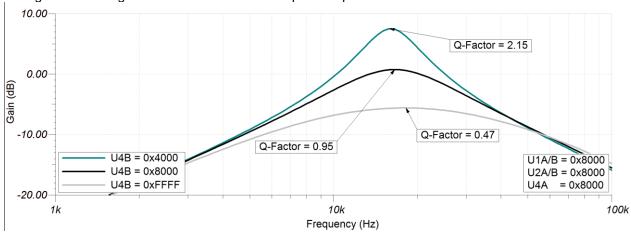


Figure 8: Quality Factor simulation – Band pass output



5 PCB Design

The PCB schematic and bill of materials can be found in the Appendix A.

5.1 PCB Layout

General PCB layout best-practices should be followed for this design. Analog and digital lines must not be traced out parallel to each other in order to reduce the coupling of digital signals onto analog signal paths.

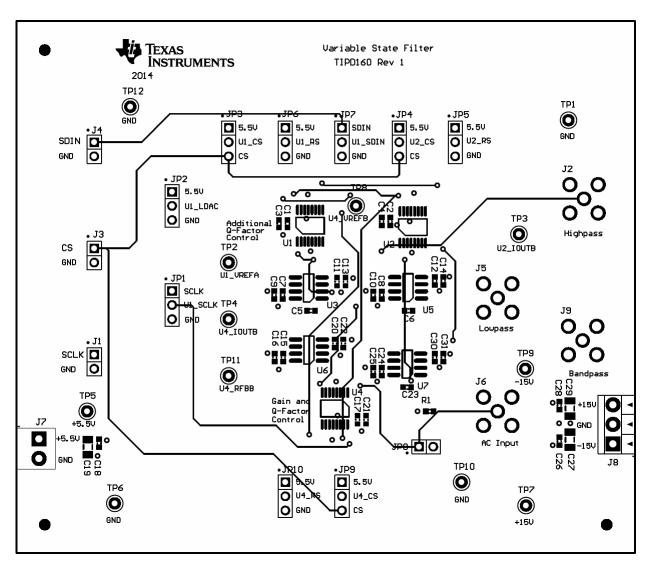


Figure 9: PCB Layout



6 Measurement

The circuit was tested using a bode plot analyzer that provided the input stimulus and measured the output response.

6.1 Center/Cut-off Frequency Measurement

The cut-off frequency setting is directly proportional to the DAC code of U2A/B. Each LSB change will adjust the frequency by approximately 0.5 Hz. For frequency measurement data for band pass and low pass filters refer to Appendix B.

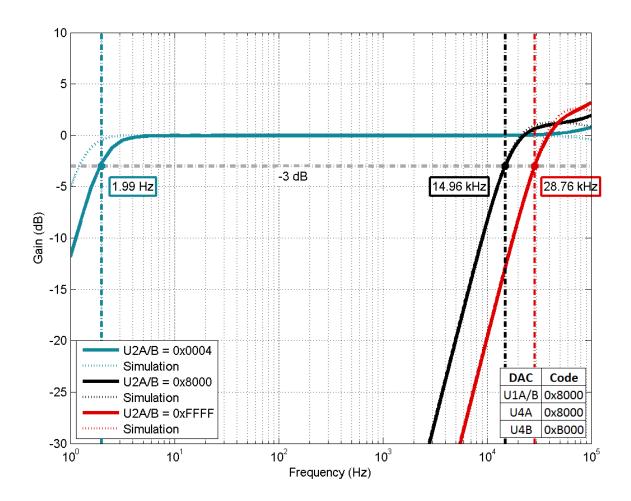


Figure 10: Cut-off frequency measurement - High pass output

Table 3. High Pass Frequency Results @ 2 kHz

| Code | Simulated Freq. | Measured Freq. | Error |
|--------|-----------------|----------------|---------|
| 0x0004 | 2.1100 Hz | 1.9900 Hz | -5.69 % |
| 0x8000 | 14690 Hz | 14962 Hz | -1.85 % |
| 0xFFFF | 27980 Hz | 28757 Hz | -2.78 % |



6.2 Gain Measurement

The gain setting is directly proportional to the DAC code of U4A. Each LSB change will adjust the gain by approximately 1 mdB. Measurements at very low codes are susceptible to noise. For gain measurement data for band pass and high pass filters refer to Appendix B.

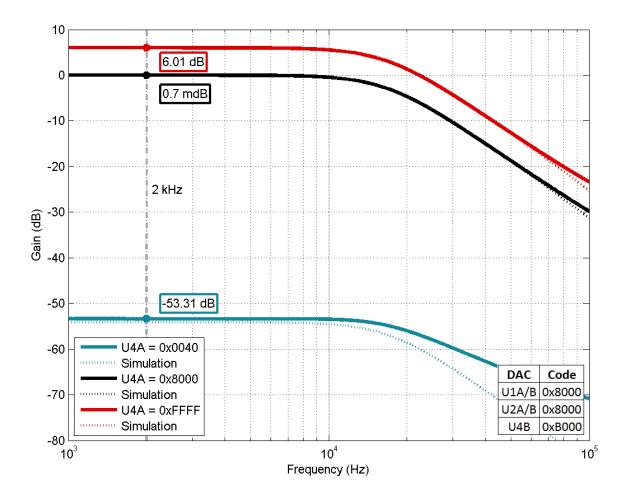


Figure 11: Gain measurement – Low pass output

Table 4. Low Pass Gain Results

| Code | Simulated Gain | Measured Gain | Error |
|--------|----------------|---------------|------------|
| 0x0040 | -54.1276 dB | -53.3100 dB | -0.8176 dB |
| 0x8000 | 0.0012 dB | 0.0007 dB | 0.0004 dB |
| 0xFFFF | 6.0200 dB | 6.0140 dB | 0.0060 dB |



6.3 Quality Factor Measurement

The quality factor measurement is inversely proportional to the DAC code of U4B. Each LSB change will adjust the quality factor by approximately 52µ. The quality factor can be controlled independently of gain by using another MDAC to control resistors R5 & R6. For information about how to calculate quality factor, please refer to Appendix B.

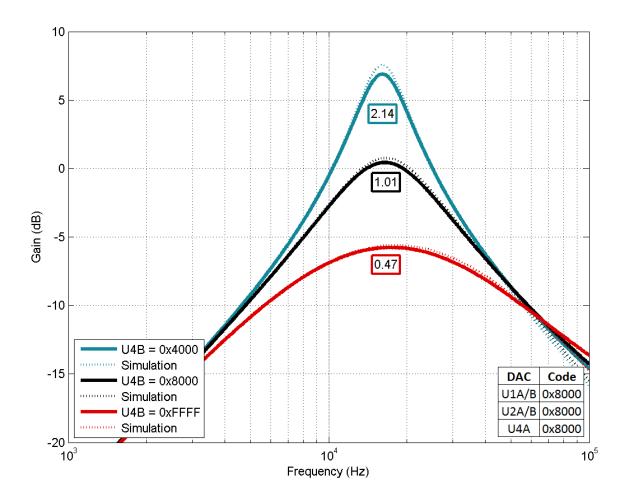


Figure 12: Quality factor measurement - Band pass output

Table 5. Band Pass Quality Factor Results

| Code | Simulated Q-Factor | Measured Q-Factor | Error |
|--------|--------------------|-------------------|---------|
| 0x4000 | 2.1524 | 2.1424 | -0.46 % |
| 0x8000 | 0.9461 | 1.0077 | 6.52 % |
| 0xFFFF | 0.4691 | 0.4660 | -0.65 % |



7 Modifications

Depending on the design requirement other multiplying DACs can be used in this design. DAC8812 was selected for its serial interface, high resolution, and superior multiplying bandwidth. Table 6 shows other MDAC options for application that may not require high resolution or that may require a parallel interface. Table 7 shows alternative amplifiers that can be used in this design for larger bandwidth or minimal input bias current.

Table 6. Alternative MDACs

| MDAC | Resolution | Channel Count | Interface | Reference multiplying bandwidth |
|---------|------------|----------------------|-----------|---------------------------------|
| DAC8812 | 16 bits | 2 | Serial | 10 MHz |
| DAC8822 | 16 bits | 2 | Parallel | 10 MHz |
| DAC8802 | 14 bits | 2 | Serial | 10 MHz |
| DAC8805 | 14 bits | 2 | Parallel | 10 MHz |
| DAC7822 | 12 bits | 2 | Parallel | 10 MHz |

Table 7. Alternative operational amplifiers

| Amplifier | Supply | Bandwidth | Input bias current (Typ.) |
|-----------|--------|-----------|---------------------------|
| OPA277 | ±18 V | 1 MHz | ±500 nA |
| OPA211 | ±18 V | 80 MHz | ±50 nA |
| OPA188 | ±18 V | 2 MHz | ±160 pA |
| OPA170 | ±18 V | 1.2 MHz | ±8 pA |

8 About the Author

Rahul Prakash is a design and systems engineer in the precision digital to analog converters group at Texas Instruments. Rahul received his BTech in Electrical and Electronics Engineering from the Netaji Subhas Institute of Technology, India, and MS in Electrical Engineering from University of Texas at Dallas.

Eugenio Mejia is an applications engineer in the precision digital to analog converters group at Texas Instruments. Eugenio received his Bachelors of Science in Electrical Engineering from Texas A&M University.



9 Acknowledgements & References

- 1. Engineer It, What is a multiplying DAC (MDAC)? (Video)
- 2. Build a three phase sine wave generator with the UAF421 (SBFA013)
- 3. Design a 60 Hz notch filter with the UAF42 (SBFA012)
- 4. TLC7528, Digitally-controlled state-variable filter application information (SLAS062E)
- 5. TIPD137, ±10V 4-Quadrant Multiplying DAC (TIDU031)



Appendix A.

A.1 Electrical Schematic

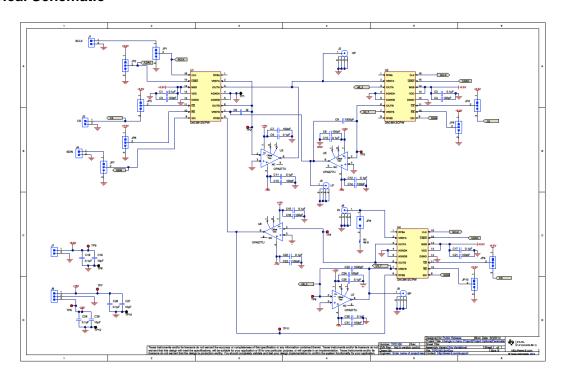


Figure A-1: Electrical Schematic

A.2 Bill of Materials



Figure A-2: Bill of Materials



Appendix B.

B.1 Center/Cut Off Frequency Simulation & Measurements

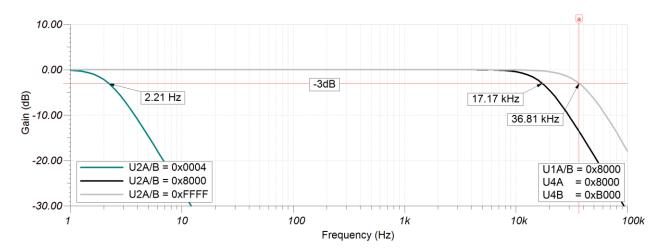


Figure B-1: Cut-off frequency simulation - Low pass output

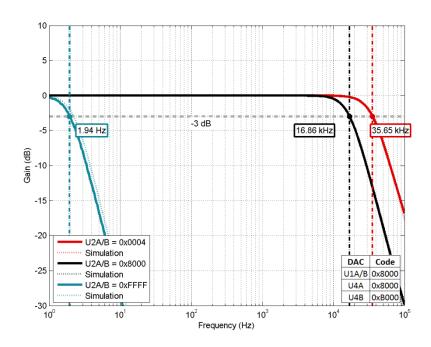


Figure B-2: Cut-off frequency measurement - Low pass output

Table 8. Low Pass Frequency Results

| Code | Simulated Freq. | Measured Freq. | Error |
|--------|-----------------|----------------|----------|
| 0x0004 | 2.2138 Hz | 1.9387 Hz | -12.45 % |
| 0x8000 | 17.1738 kHz | 16.8585 kHz | -1.84 % |
| 0xFFFF | 36.81 kHz | 35.6480 kHz | -3.16 % |



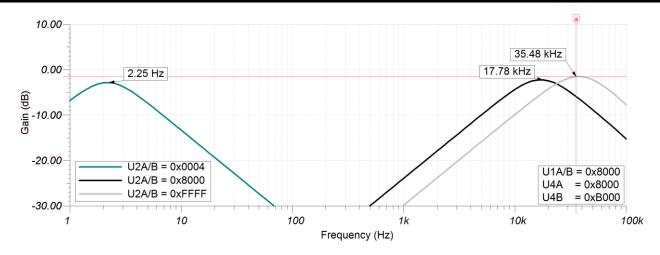


Figure B-3: Cut-off frequency simulation - Band pass output

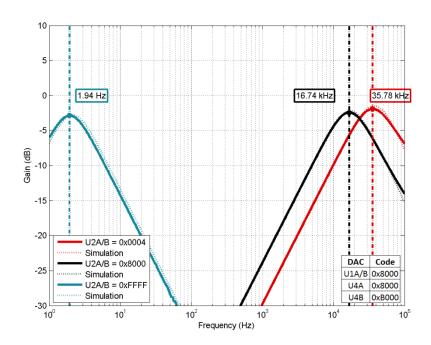


Figure B-4: Cut-off frequency measurement – Band pass output

Table 9. Band Pass Frequency Results

| Code | Simulated Freq. | Measured Freq. | Error |
|--------|-----------------|----------------|----------|
| 0x0004 | 2.2514 Hz | 1.9387 Hz | -13.89 % |
| 0x8000 | 17.7834 kHz | 16.7400 kHz | -5.87 % |
| 0xFFFF | 35.4852 kHz | 35.7890 kHz | 0.86 % |

B.2 Gain Simulation & Measurements

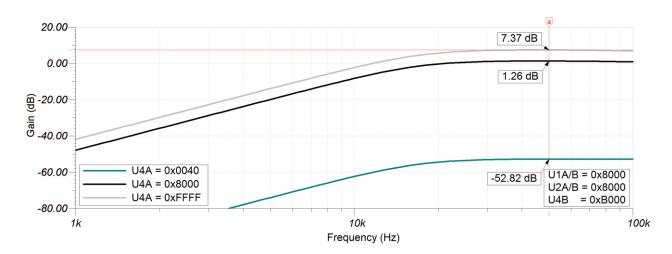


Figure B-5: Gain simulation - High pass output

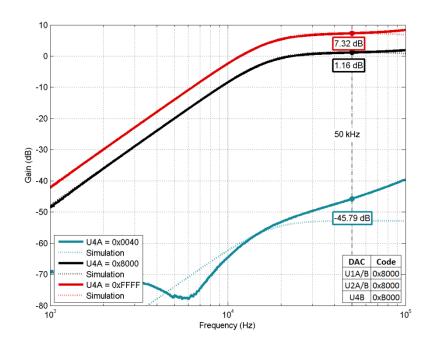


Figure B-6: Gain measurement – High pass output

Table 10. High Pass Gain Results @ 50 kHz

| Code | Simulated Gain | Measured Gain | Error |
|--------|----------------|---------------|----------|
| 0x0004 | -52.8254 dB | -45.7880 dB | -7.04 dB |
| 0x8000 | 1.2612 dB | 1.1631 | 0.10 dB |
| 0xFFFF | 7.3731 dB | 7.3293 | 0.04 dB |



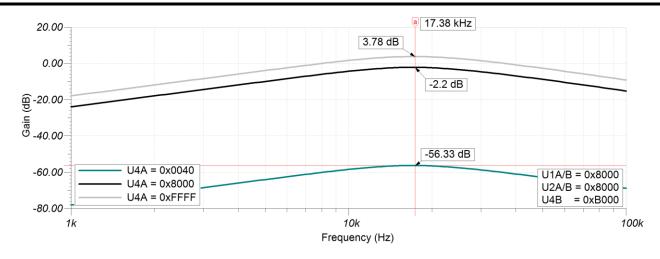


Figure B-7: Gain simulation-Band pass output

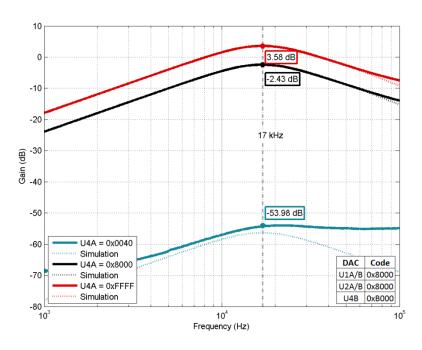


Figure B-8: Gain measurement – Band pass output

Table 11. Band Pass Gain Results

| Code | Simulated Gain | Measured Gain | Error |
|--------|----------------|---------------|----------|
| 0x0004 | 3.7835 dB | 3.5845 dB | 0.20 dB |
| 0x8000 | -2.2214 dB | -2.4316 dB | 0.21 dB |
| 0xFFFF | -56.3345 dB | -53.9780 dB | -2.36 dB |



B.3 Quality Factor Simulation & Measurements

The quality factor is calculated using Equation (9), the center frequency (f_c) and the -3 dB bandwidth (Δf. 3dB) of the bandpass filter.

$$Q = \frac{f_c}{\Delta f_{-3dB}} \tag{9}$$

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