



Control of SMPS – a Refresher

Part 1

Colin Gillmor (APP, HPC)



Control of SMPS – a Refresher:

Agenda

- Part 1 {
 - 1. Concepts
 - 2. Transfer Functions
 - 3. Control Systems
 - Part 2 {
 - 4. Loop Transfer Functions
 - Control to Output: $G(s)$
 - Output to Control: $H(s)$
 - 5. Loop Compensation
 - Part 3 {
 - 6. Measuring the Control Loop
 - 7. Summary and other issues
 - 8. References
- Power Stage (Plant)
Feedback (Control)



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Power Stage (Plant)

Feedback (Control)

Concepts:

Controllability:

- What variables can we use to control the system's state
- Eg: **Switching Frequency, Duty Cycle, Handlebars**

Observability:

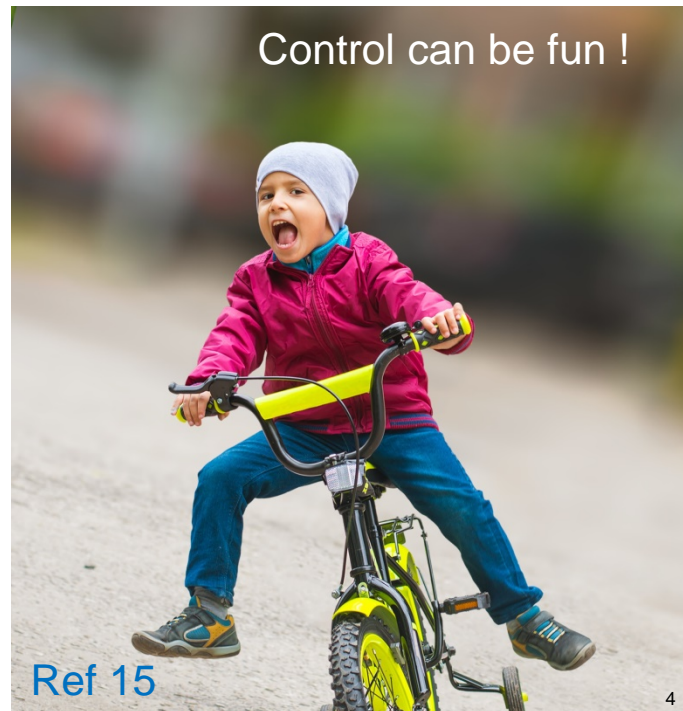
- How can we determine the system's state
- Eg: **Measure V_{out} , V_{in} , I_{out} , Inductor Current, Eyes**

Reachability:

- Does the control system have enough authority to do what we want it to do?
- Eg: **Transient response, Trim range, Current limit
Start-up time, Lean limits (aka, training wheels)**

Control:

- Measure the system
- Compare to reference
- Adjust appropriately



Concepts: LTI, Linear Time-Invariant

Linearity $f(a+b) = f(a) + f(b)$, $f(k*a) = k*f(a)$

- System response doesn't depend on the load power or current
- Non-Linear at OCP, OVP, Enhanced Dynamic Response etc

Time Invariance

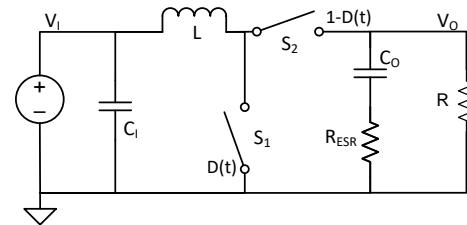
- System does not change with time
- Exceptions at power up, power down, OCP etc
- Switching action in power stage must be averaged

Continuous time assumed

- Time variable is continuous and can take up any value
- Assumption is valid up to about 20% of switching frequency

Switching frequency does not appear in the transfer function !

SMPS are not linear and are not time invariant !



So we 'cheat' and build a model which is LTI 😊

- Linearisation
- State Space Averaging

$$G(s) = A_{VC} \cdot \frac{1 + \frac{s}{\omega_z}}{1 + \frac{s}{Q_0 \cdot \omega_0} + \frac{s^2}{\omega_0^2}}$$

Typical Buck Converter model

Concepts: Complex Frequency (s)

Complex Frequency: $s = \sigma + j\omega$

σ sets decay rate,

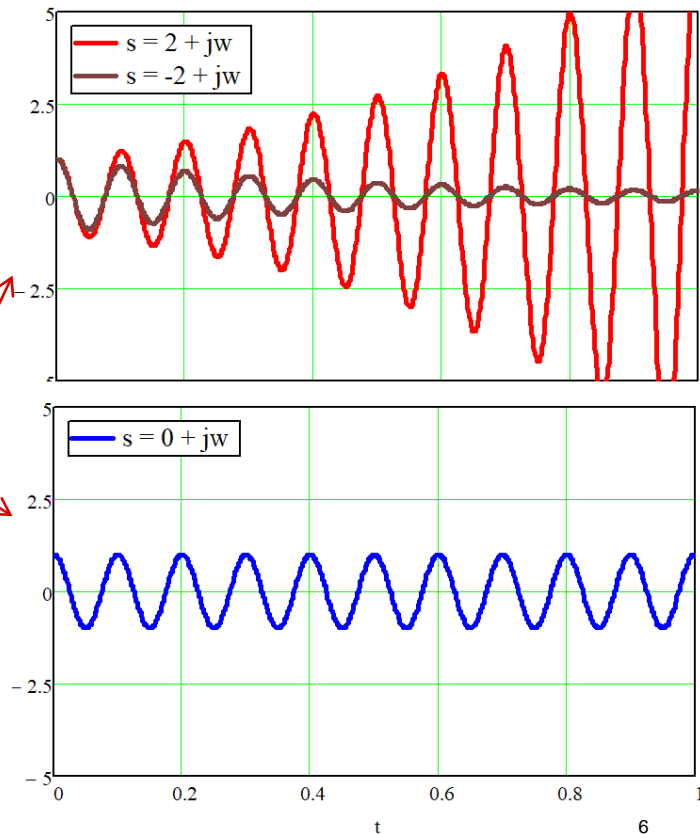
- $\sigma > 0$, increasing: $\sigma < 0$, decaying: $\sigma = 0$, steady state
- We set σ to 0 and so that $s = j\omega$
- ω is the frequency of the underlying sine wave

$$V_i(t) = \text{Re}\left(V_m \cdot e^{\sigma \cdot t} \cdot \cos(\omega \cdot t + \varphi)\right)$$

$y(s)$ contains Magnitude and Phase information.

Really useful property – a single calculation gives


- Magnitude = $\text{Mag}[y(s)]$,
- Phase = $\text{arg}[y(s)]$ (radians !)





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Transfer Functions: Bode Plots

The transfer function is basically $V_o(s) / V_i(s)$

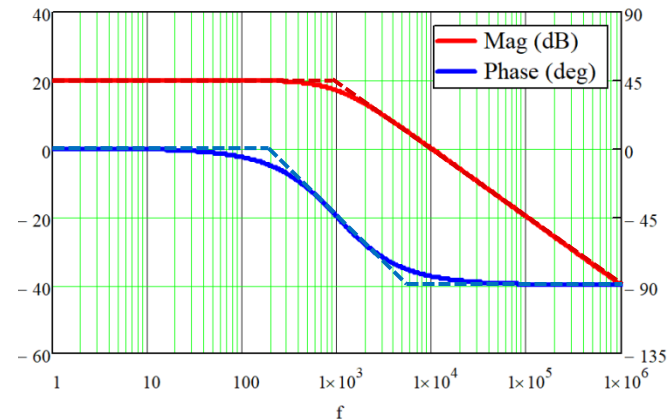
- $H(s)$, $G(s)$, $Y(s)$ etc, etc,
- Calculated or Measured
- A function frequency
- Complex frequency gives Magnitude and Phase

Bode Plot, Magnitude and Phase versus frequency

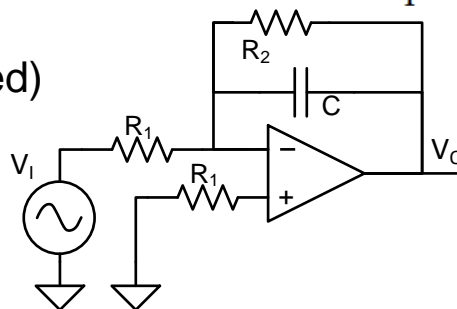
- Frequency is on a Log scale
- Magnitude in dB: $20 \log (V_o/V_i)$
- Phase in deg: $\theta_{IN} - \theta_O$
- Can use straight line approximations (dotted)

Note

- Magnitude, Amplitude, Gain are equivalent



$$G(s) = \frac{-R_2}{R_1} \cdot \frac{1}{1 + \frac{s}{\omega_p}} \quad \text{where} \quad \omega_p = \frac{1}{R_2 \cdot C}$$



Transfer Functions: Poles

$$G(s) = \frac{-R_2}{R_1 \cdot (R_2 \cdot sC + 1)} = \frac{-R_2}{R_2} \cdot \frac{1}{1 + sCR_2} = \frac{-R_2}{R_1} \cdot \frac{1}{1 + \frac{s}{\omega_0}}$$

$$G(s) = \frac{-R_2}{R_1} \cdot \frac{1}{1 + \frac{s}{\omega_0}}$$

where $\omega_0 = \frac{1}{R_2 \cdot C}$

LF gain is $-R_2/R_1$

Gain rolls off at -20dB per decade above ω_0

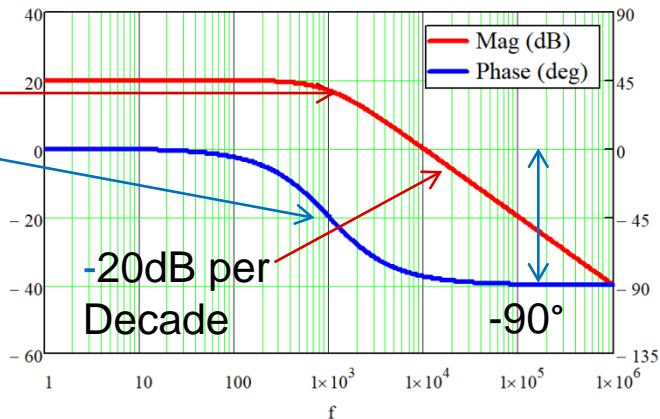
Gain is flat below ω_0

Phase flat below $\omega_0 / 10$ and above $10 \omega_0$

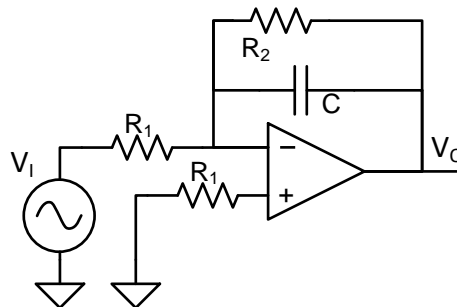
Phase is:

- 0° at LF
- -45° at ω_0
- -90° at HF

Pole
-3dB
-45°



Gain is -3dB at ω_0 $f_p = \frac{1}{2\pi R_2 C}$





Transfer Functions: Zeros

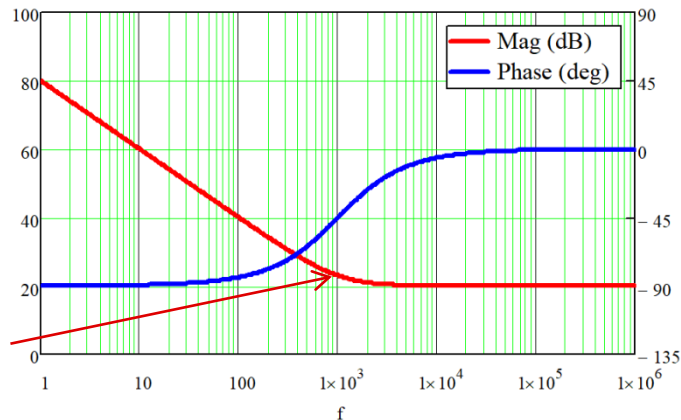
$$G(s) = \frac{-z_1}{z_2} = \frac{-\left(R_2 + \frac{1}{sC_1}\right)}{R_1} = \frac{-R_2}{R_1} \left(1 + \frac{1}{sCR_2}\right) = \frac{-R_2}{R_1} \left(1 + \frac{\omega_Z}{s}\right)$$

$$G(s) = \frac{-R_2}{R_1} \left(1 + \frac{\omega_Z}{s}\right)$$

where

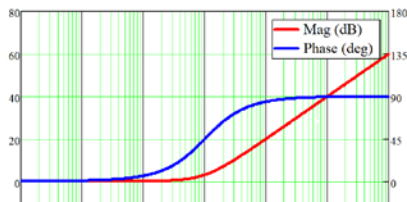
$$\omega_Z = \frac{1}{R_2 \cdot C}$$

Zero



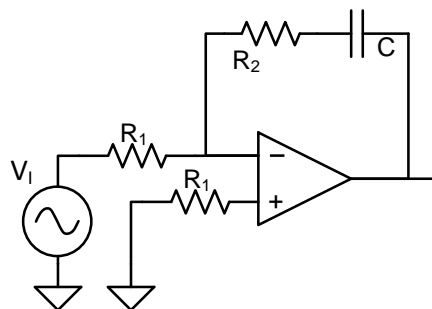
Used in Type 2 compensator to add some phase boost and so increase the phase margin

+3dB at $f_z = \frac{1}{2\pi R_2 C}$



Alternative form

$$G(s) = 1 + \frac{s}{\omega_Z}$$



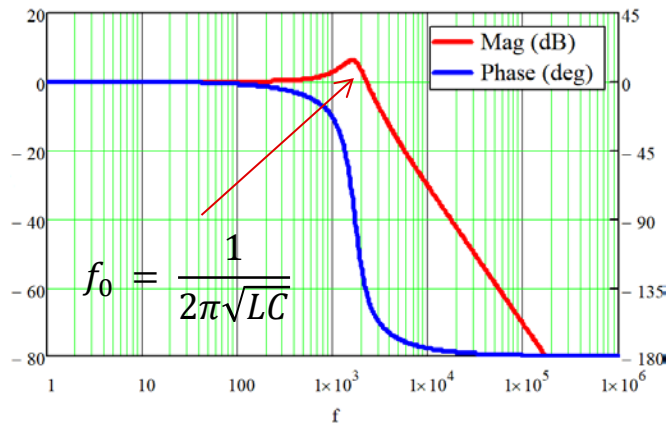
Transfer Functions: Complex Conjugate Poles

Complex Conjugate Poles: Resonance,
Phase decreasing to -180°
Q determines peak response

Gain rolls off at -40dB per decade above ω_0

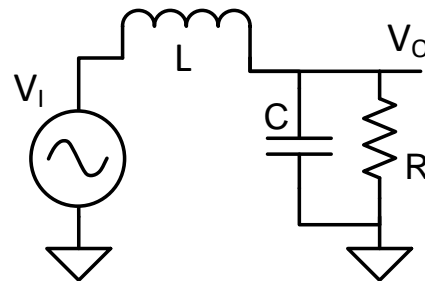
Phase is:

- 0° at LF
- -90° at ω_0
- -180° at HF



$$G(s) = \frac{1}{1 + \frac{s}{Q \cdot \omega_0} + \frac{s^2}{\omega_0^2}}$$

$$Q = \frac{R}{\sqrt{L/C}}$$



Transfer Functions: Right Half Plane Zero

RHPZ:

- A characteristic of topologies which deliver energy to the output 180° out of phase with the energy taken from the input Flyback, Boost, Cuk, (CCM only).

RHPZ: (Right Half Plane Zero)

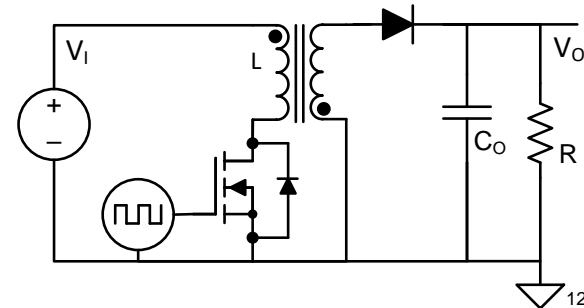
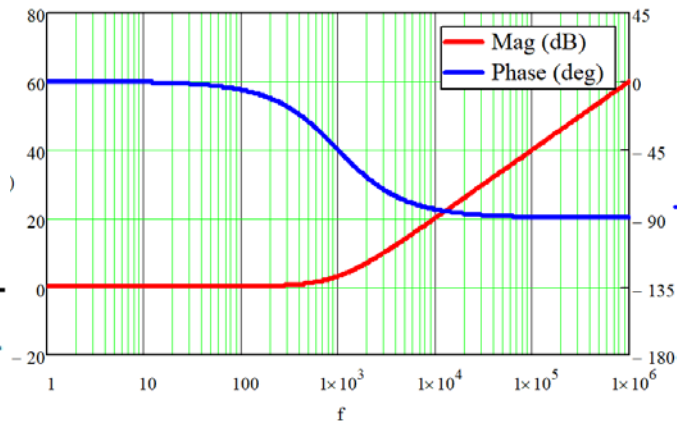
- Gain increasing Phase decreasing
- Almost impossible to compensate for this
- Must close the loop at frequencies $\ll \omega_z$

RHPZ is not an issue in Boost PFC

- They must close the loop at very low frequencies for other reasons, $\text{typ} < 10 \text{ Hz}$.
- Controlled quantity is input current, not output current

Ref 1

$$G(s) = 1 - \frac{s}{\omega_z}$$





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Control Systems: Variables

Many SMPS use Duty Cycle (D) as the control variable

- CCM, PSFB, Push-Pull

Sometimes D and F_{SW} are both used

- Mainly to improve efficiency
- Quasi Resonant, DCM converters
- Conversion ratios are unchanged

$$V_{OUT} = D \cdot V_{IN}$$

Buck Converter

$$V_{OUT} = \frac{1}{1 - D} \cdot V_{IN}$$

Boost Converter

$$V_{OUT} = \frac{D}{1 - D} \cdot V_{IN}$$

Flyback Converter

Conversion factor is a function of D, not of F_{SW}

LLC uses F_{sw} as the control variable

- One of a large class of resonant converters

$$\text{Gain}(f, Q) = \left| \frac{L_N \cdot f^2}{L_N \cdot f^2 + (f^2 - 1)(1 + j \cdot f \cdot L_N \cdot Q)} \right|$$



Conversion factor is a function of F_{SW} not of D

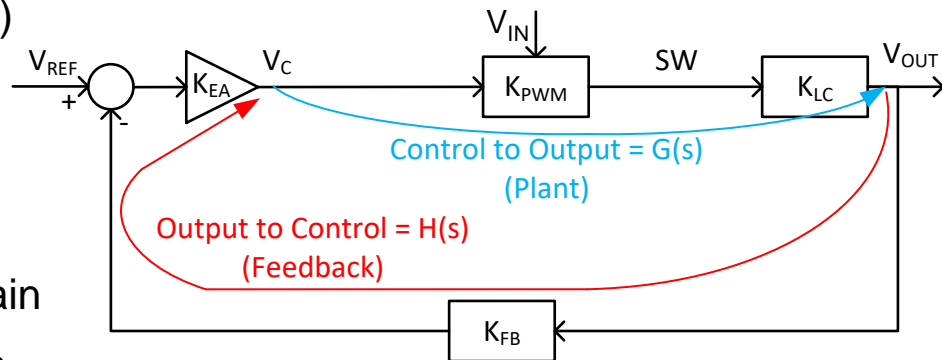
Hysteretic SMPS use Upper and Lower limits on VOUT

A Typical Control System:

A typical analog SMPS control system looks something like this [Ref 2: Ch6](#)

- $K_{EA}(s)$ * Error Amplifier (transfer function as function of complex frequency)
- K_{PWM} Pulse Width Modulator (A Constant)
- $K_{LC}(s)$ Output Filter
- K_{FB} Feedback Potential Divider

- $G(s) = K_{PWM} * K_{LC}(s) =$ Control to Output gain
- $H(s) = K_{FB} * K_{EA}(s) =$ Output to Control gain
- Total loop response $T(s) = G(s) * H(s)$



System measures the output, compares to the reference, makes an adjustment

Two Control Systems: VMC and CMC

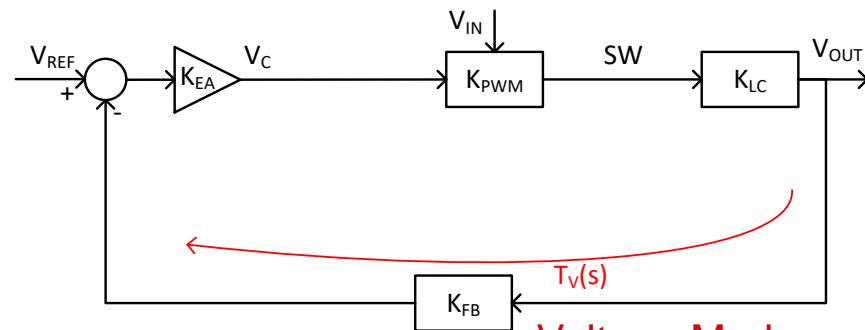
VMC:

- Error Amplifier controls Duty Cycle (D) directly

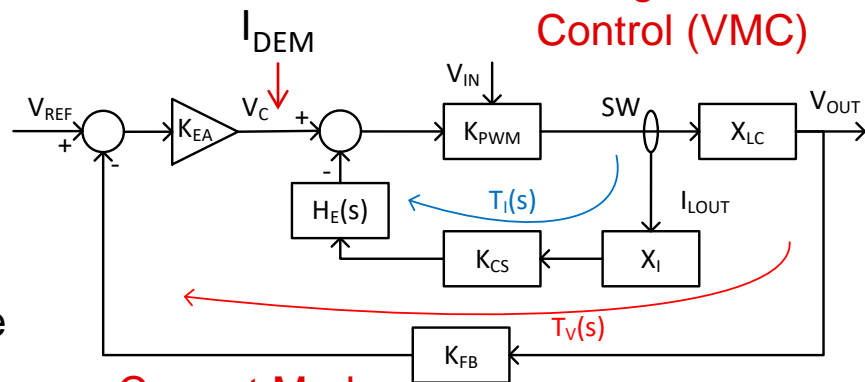
CMC:

- PCM (Peak Current Mode)
- ACM (Average Current Mode)
- Error Amplifier sets I_{DEM} (Current Demand) for inner loop. sometimes called 'COMP'
- Inner loop regulates the output current

Other control methods do exist – not covered here



Voltage Mode Control (VMC)



Current Mode Control (CMC)

Control Systems: Voltage Mode Control

Error amplifier output V_C controls D directly

V_{OUT} drops $\rightarrow V_C$ increases $\rightarrow D$ increases $\rightarrow V_{OUT}$ increases

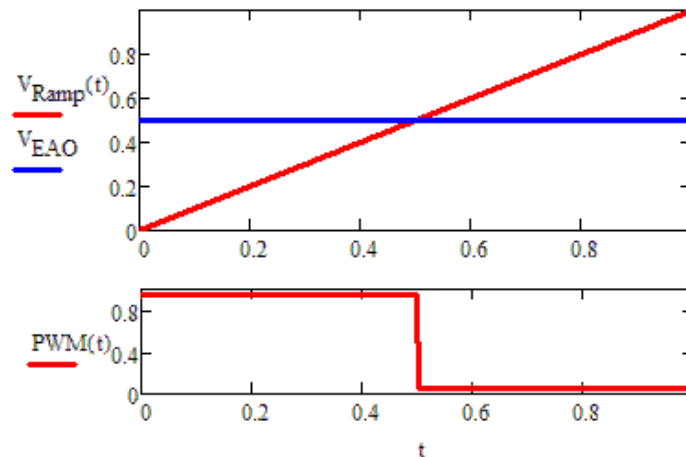
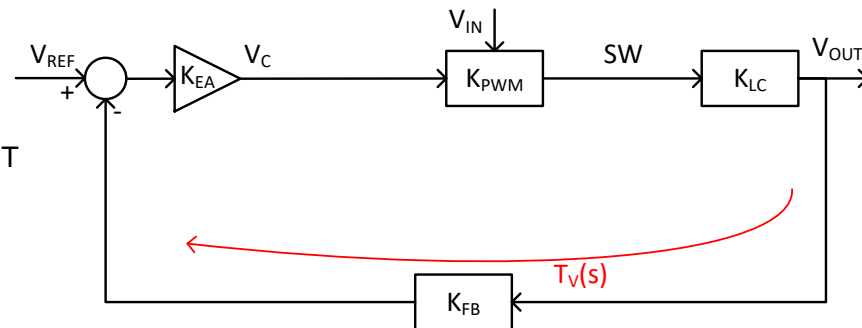
Less noise sensitive than PCM – larger ramp

Easy to implement Voltage Feed Forward

Output Filter appears in the transfer function so

- Control loop bandwidth is lower than with CMC
- More difficult to stabilise than CMC
- Type 3 Compensation (more on this later)

Just because it's more difficult to stabilise doesn't mean that it is impossible to stabilise.



Control Systems: Current Mode Control

Peak Current Mode – most common

Average Current Mode – used in some PFC stages

Error amplifier output V_C sets a current demand

Inner current loop forces the output current to equal the current demand.

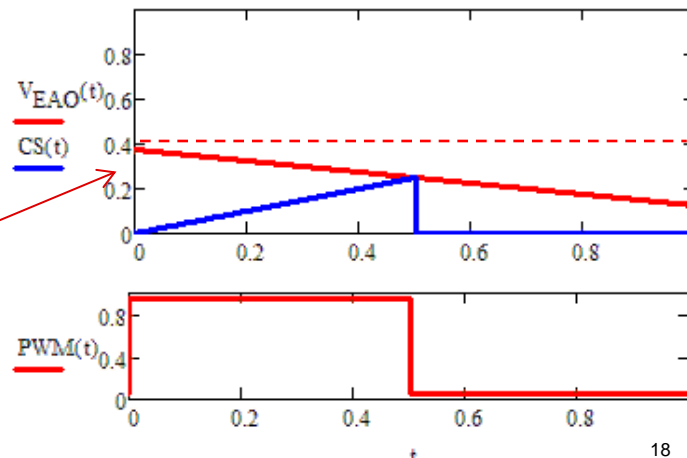
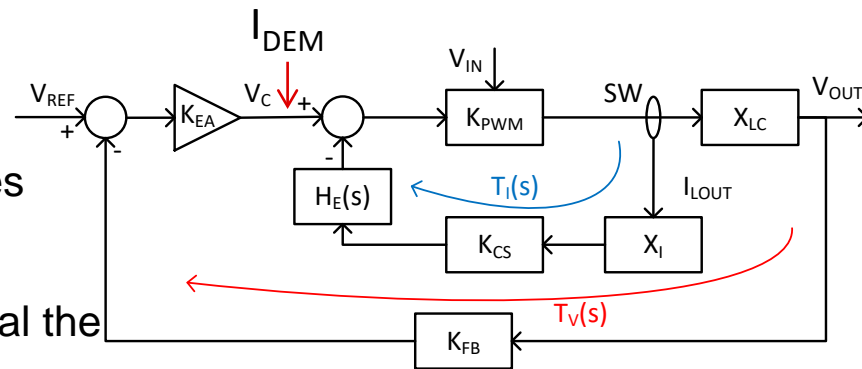
V_{OUT} drops $\rightarrow V_C$ (I_{DEM}) increases, I_{OUT} increases $\rightarrow V_{OUT}$ increases

Wider loop bandwidth and easier to stabilise than VMC

Cycle-by-Cycle over current protection

Sub-Harmonic instability, (PCM in CCM)

- Slope Compensation (added to V_{EAO})
- Peak-to-Average ratio not constant – distortion in PFC



Control Systems: PCM Half Bridge instability

Peak Current Mode control of half bridge is unstable

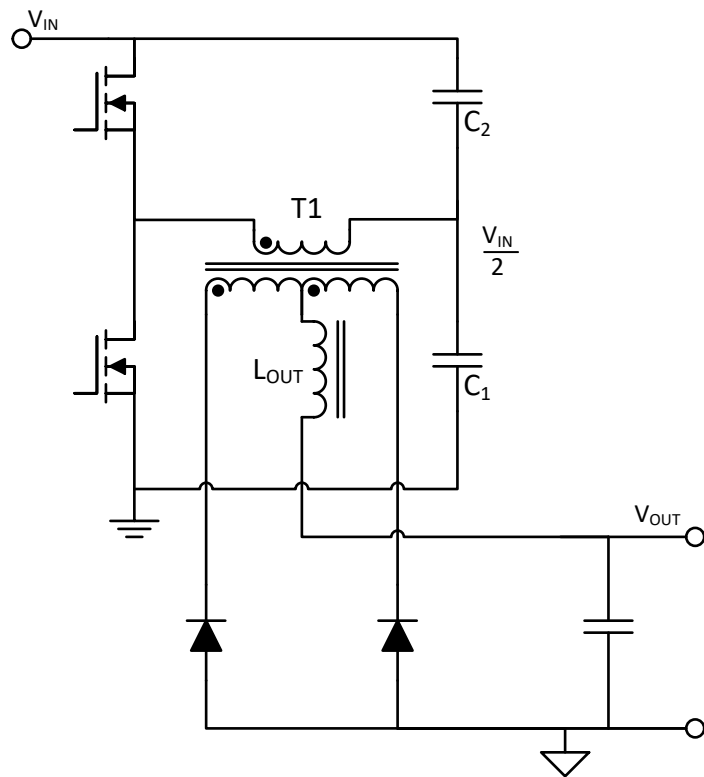
Described in [Ref 13](#)

Voltage at centre point of C_1 and C_2 diverges from $V_{IN}/2$

- This is an inherent instability

Solutions

- Use VMC – any half bridge controller
- Use duty cycle copy – UCC28251
- Use Average current limit - LM5039
- Modified CT circuit – see article above





References

- 1/ The Right Half plane Zero, A Simplified Explanation, Dixon: <https://www.ti.com/seclit/ml/slup084/slup084.pdf>
- 2/ Fundamentals of Power Supply Design: Mammano: Texas Instruments, 2017
- 3/ SMPS compensation made easy, Sheehan: <https://www.ti.com/seclit/ml/slup340/slup340.pdf>
- 4/ Control Loop Cookbook, Dixon: <https://www.ti.com/seclit/ml/slup113/slup113.pdf>
- 5/ Compensation Design with TL431 for UCC28600: <http://www.ti.com/lit/an/slua671/.pdf>
- 6/ Designing with the TL431, Ridley: https://www.researchgate.net/publication/280308828_Designing_with_the_TL431_-_the_first_complete_analysis
- 7/ A more Accurate Current-Mode Control Model, Ridley: <https://www.ti.com/seclit/ml/slup122/slup122.pdf>
- 8/ Modelling, Analysis and Compensation of the Current Mode Converter: <http://www.ti.com/lit/an/slua101/slua101.pdf>
- 9/ Average Current Mode Control of Switching Power Supplies, Dixon: <https://www.ti.com/seclit/ml/slup091/slup091.pdf>
- 10/ Considerations for measuring loop gain in power supplies: <https://www.ti.com/seclit/ml/slup386/slup386.pdf>
- 11/ Fundamentals of Power Electronics: Erickson and Maksimovic, ISBN 0-7923-7270-0
- 12/ Modern Control Systems: Dorf, Addison Wesley, ISBN: 0-201-51713-2
- 13/ http://www.how2power.com/pdf_view.php?url=/newsletters/1204/articles/H2PToday1204_design_TexasInstruments.pdf
- 14/ <http://venable.biz/uploads/files/01-Technical-Paper-Testing-Power-Sources-for-Stability.pdf>
- 15/ https://en.wikipedia.org/wiki/Bicycle_and_motorcycle_dynamics



Control of SMPS – a Refresher

End of Part 1

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Control of SMPS – a Refresher

Part 2

Colin Gillmor (APP, HPC)



Control of SMPS – a Refresher:

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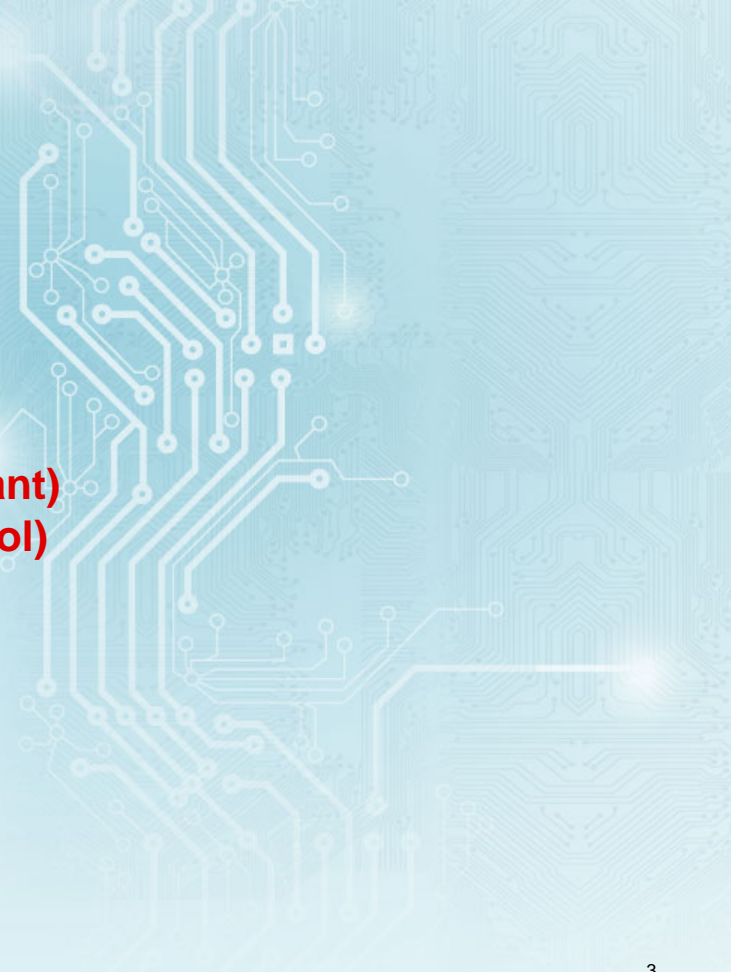
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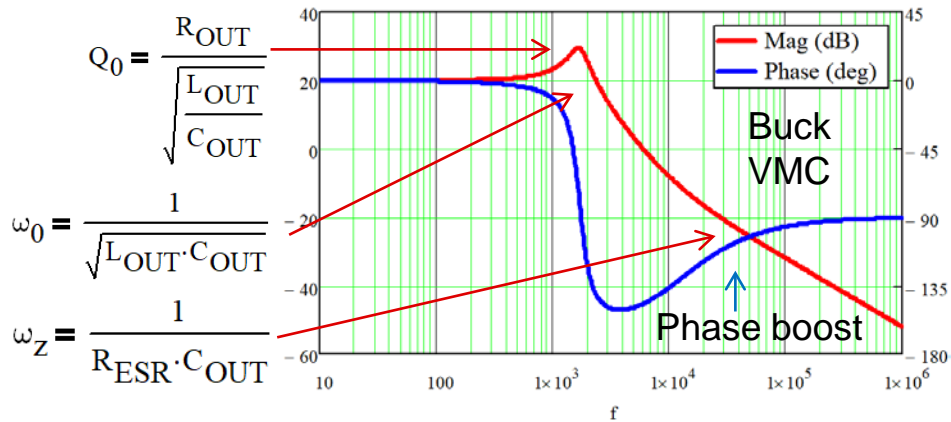
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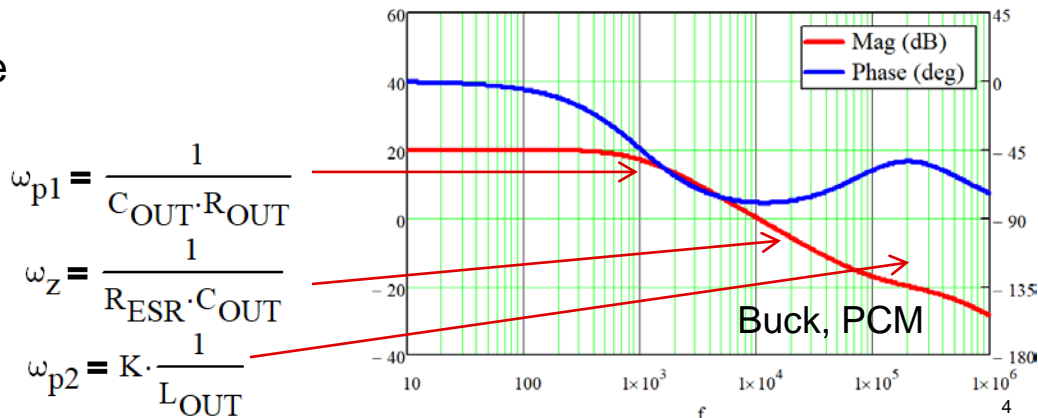


Control to Output Transfer Function: $G(s)$

- $G(s) = \frac{V_{OUT}}{V_C} = K_{PWM} * K_{LC}(s)$
- Buck Converter in Voltage Mode Control
- Output Inductor/Capacitor resonance
- Phase boost, zero of ESR and Cout
- Type 3 compensation needed (more later)



- Buck Converter in Peak Current Mode
- First order characteristic
- Phase boost, zero of ESR and Cout
- Type 2 compensation (more later)
- Ref 3





Control to Output Transfer Function: G(s)

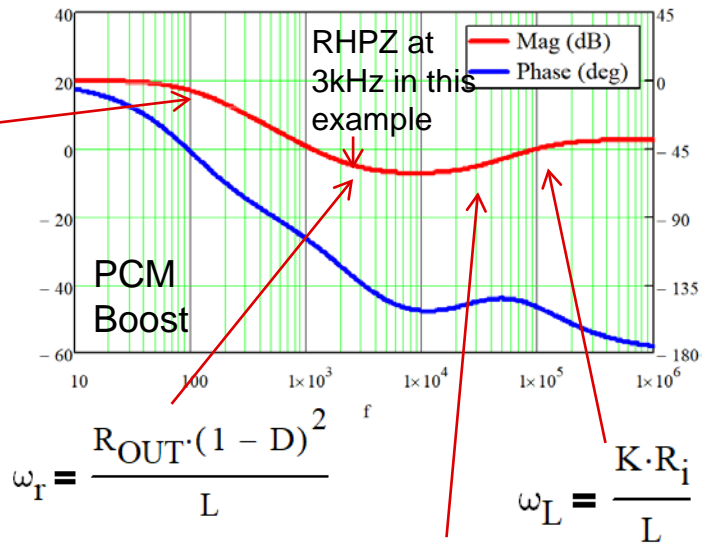
$$G(s) = \frac{V_{OUT}}{V_C} = K_{PWM} * K_{LC}(s)$$

$$\omega_p = \frac{2}{C_{OUT} \cdot R_{OUT}}$$

A right-half-plane zero appears in the transfer function of topologies which deliver energy to the output 180° out of phase with the energy taken from the input.

(in CCM only, Flyback, Boost, Cuk topologies)

(Sheehan: slup340 and Dixon: slup084)



$$\omega_r = \frac{R_{OUT} \cdot (1 - D)^2}{L}$$

$$\omega_L = \frac{K \cdot R_i}{L}$$

$$\omega_z = \frac{1}{R_{ESR} \cdot C_{OUT}}$$

Remember - RHPZ: Gain increasing Phase decreasing

- Severely limits the control bandwidth

Flyback transfer function under PCM

$$G(s) = A_{VC} \cdot \frac{\left(1 - \frac{s}{\omega_r}\right) \cdot \left(1 + \frac{s}{\omega_z}\right)}{\left(1 + \frac{s}{\omega_p}\right) \cdot \left(1 + \frac{s}{\omega_L}\right)}$$

Output to Control Transfer Function: $H(s)$

This is the feedback system used to close the control loop

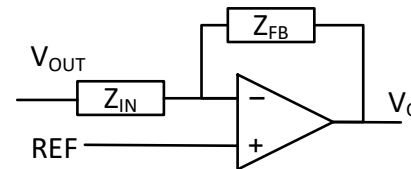
We need

- 180deg phase shift at DC for negative feedback
- High gain at DC, for good regulation
- High loop bandwidth, for good transient response (except PFC)
- Adequate gain and phase margins, for stability
PM > 45° at 0dB gain

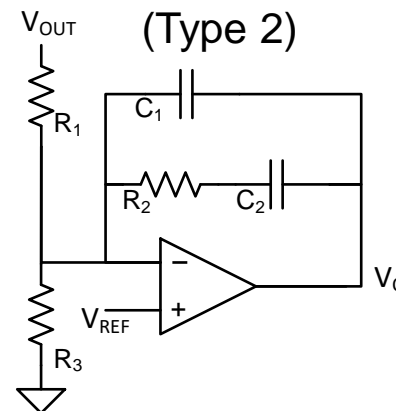
Need to reduce gain to less than 1 before $\approx f_{sw}/10$

- Prevent the control loop from 'seeing' the switching action
- Ideally gain dropping at -20dB per decade at the cross over
- Makes system less sensitive to component variations

Error Amplifier



More Detail (Type 2)





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The Feedback Network: $H(s)$

Three generic types of Compensation network

Type 1, 1 pole at origin, no phase boost

Type 2, 1 pole at origin, 1 zero, 1 HF pole,

- phase boost up to 90°

Type 3, 1 pole at origin, 1 zero pair, 1 HF pole pair,

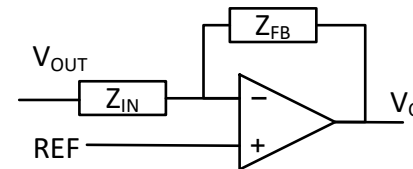
- phase boost up to 180°

The terms PI, PID are used in digital control systems

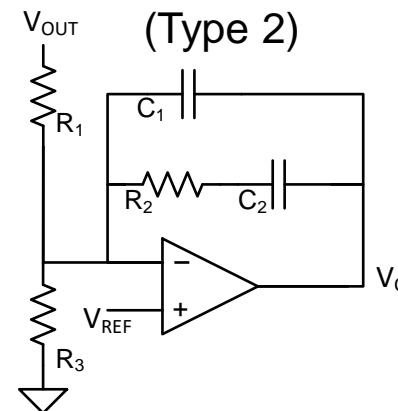
Similar but no direct correlation to the Type 1, 2, 3 classification used here.

Ref 3 **VERY** Highly Recommended

Error Amplifier



More Detail
(Type 2)



Loop Response: Requirements for Stability

Loop Stability: Remember: 0dB = gain of 1

- There is a 180deg phase shift at DC
- System will oscillate (at the crossover frequency) if there is an ADDITIONAL 180° around the loop at the crossover frequency. Ref 4

For Stability

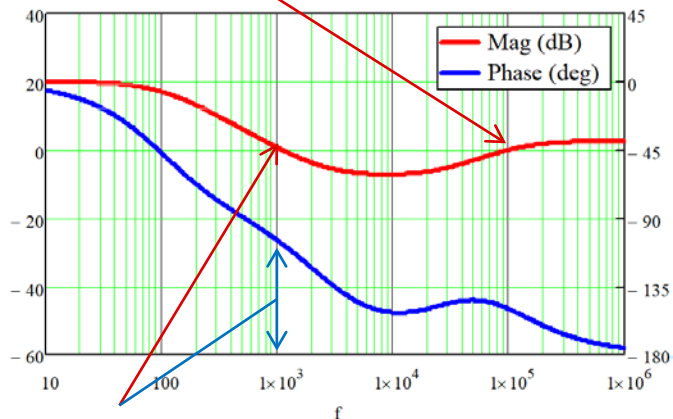
- Phase must be $< 180^\circ$ when the gain goes through 0dB
- Gain must be < 0 dB when the phase goes through 180°

Compensation network must be designed for

- Adequate gain and phase margins, for stability
- PM $> 45^\circ$ at 0dB gain

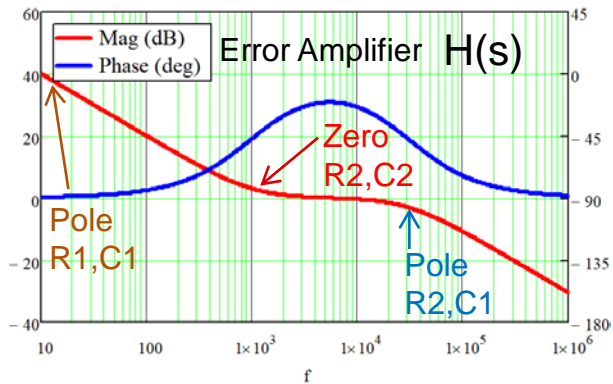
Need to reduce gain to less than 0dB before $\approx f_{sw}/10$

Metastable condition if gain pops up above 0dB
To be avoided !



0dB crossover at 1kHz
Phase Margin $\approx 76^\circ$

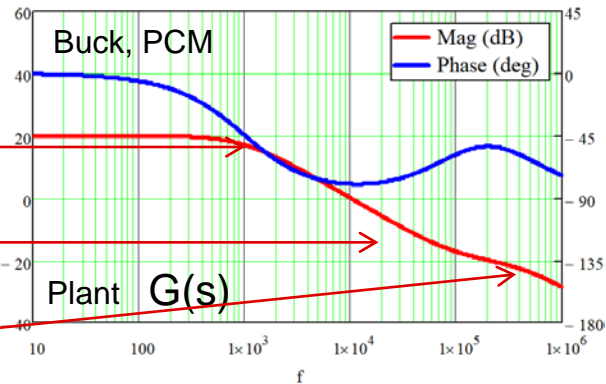
Loop Response: $T(s) = H(s)G(s)$, Buck PCM



$$\omega_{p1} = \frac{1}{C_{OUT} \cdot R_{OUT}}$$

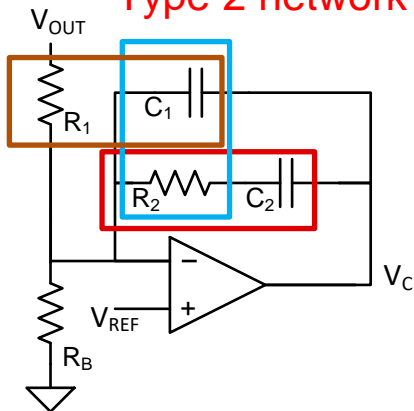
$$\omega_z = \frac{1}{R_{ESR} \cdot C_{OUT}}$$

$$\omega_{p2} = K \cdot \frac{1}{L_{OUT}}$$



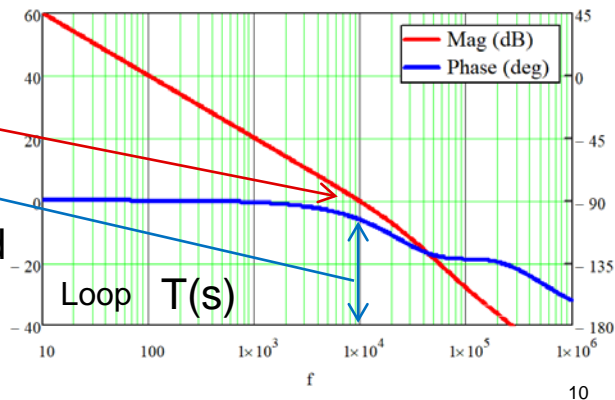
LF Pole

Type 2 network

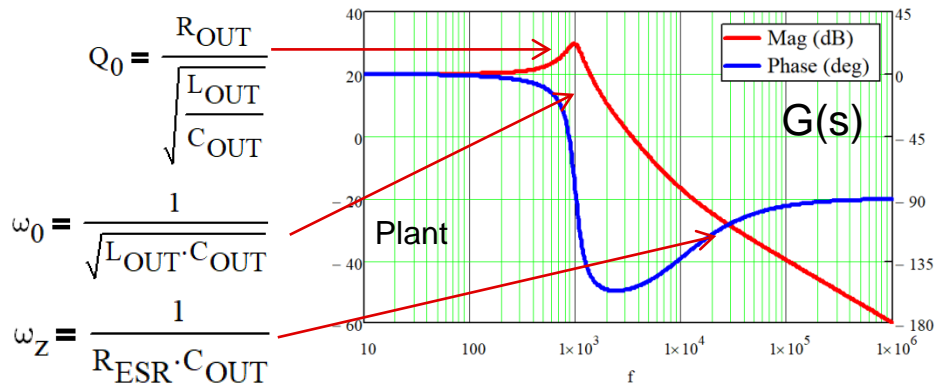
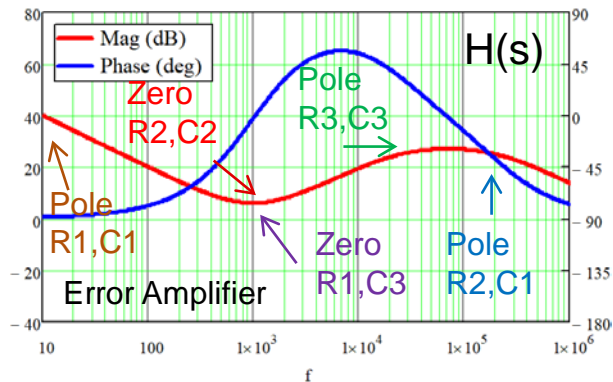


- Loop crossover at 10kHz
- Approx. 76° phase margin
- Inverting input is virtual ground
- R_B attenuates V_{out} only

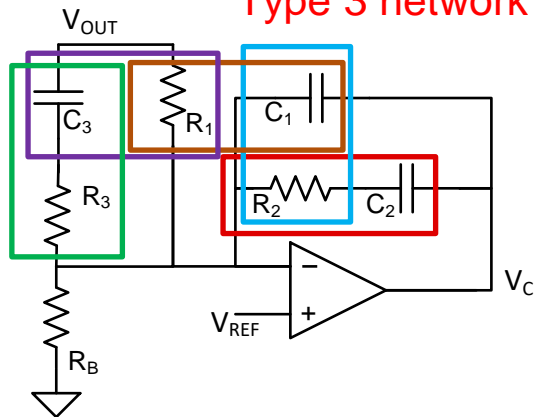
Ref 3



Loop Response: $T(s) = H(s)G(s)$, Buck VMC

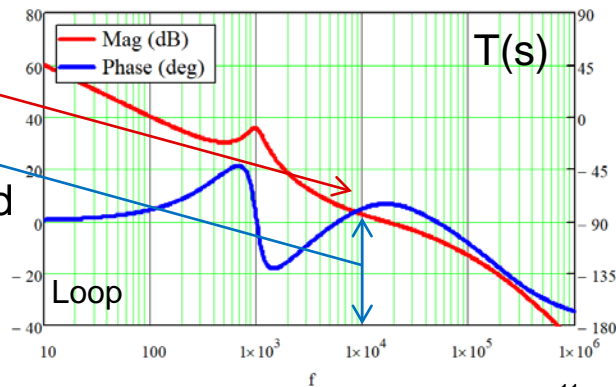


Type 3 network



- Loop crossover at 10kHz
- Approx. 90° phase margin
- Inverting input is virtual ground
- R_B attenuates V_{out} only

Ref 3



The TL431:

Reference + Error Amplifier in one IC

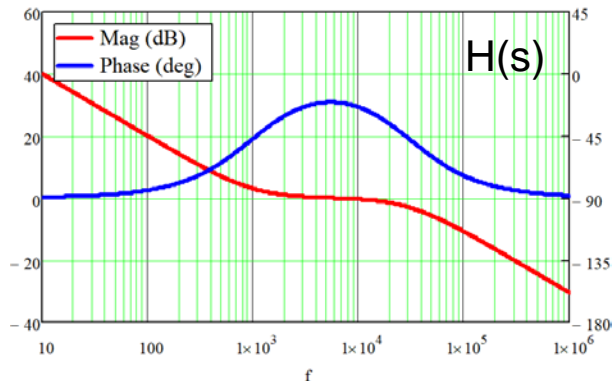
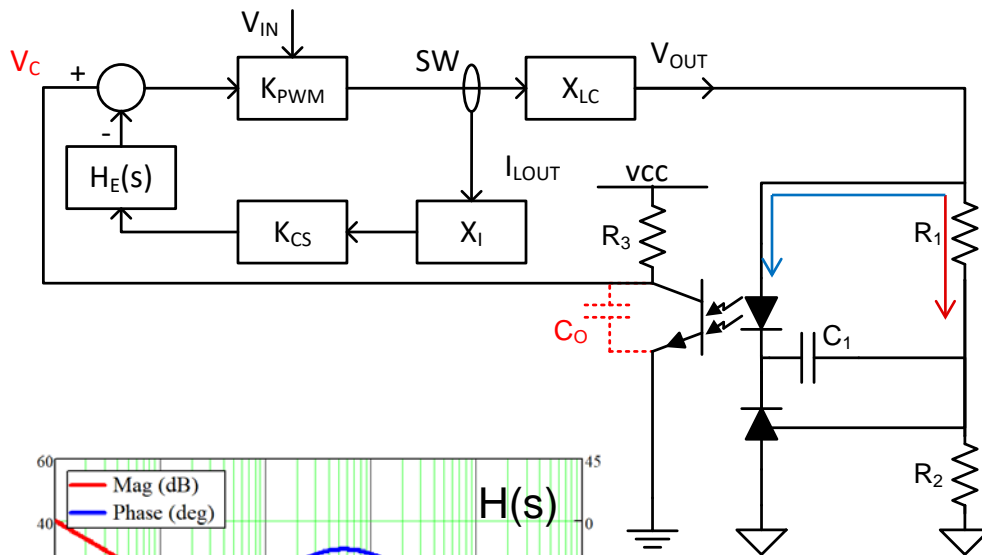
Type 2 compensator shown here,

- 1 pole at origin,
- 1 zero,
- 1 HF pole, phase boost up to 90°

Ref 5

Ref 6 (VERY highly Recommended)

- Optocoupler has pole due to parasitic output capacitance C_O



Pole at origin,
Zero, $R_1 C_1$
HF pole at $R_3 C_O$

The TL431:

High V_{OUT} ($> \approx 36V$) or Low V_{OUT} ($< \approx 3V$)

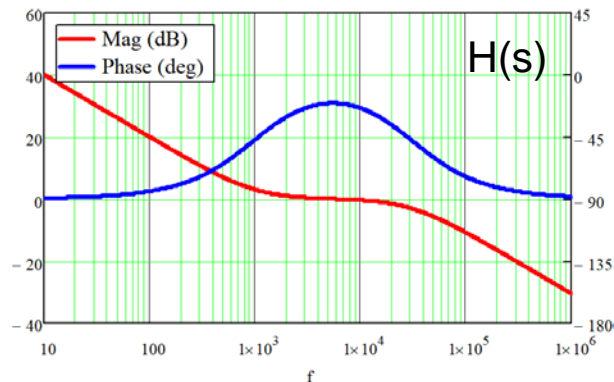
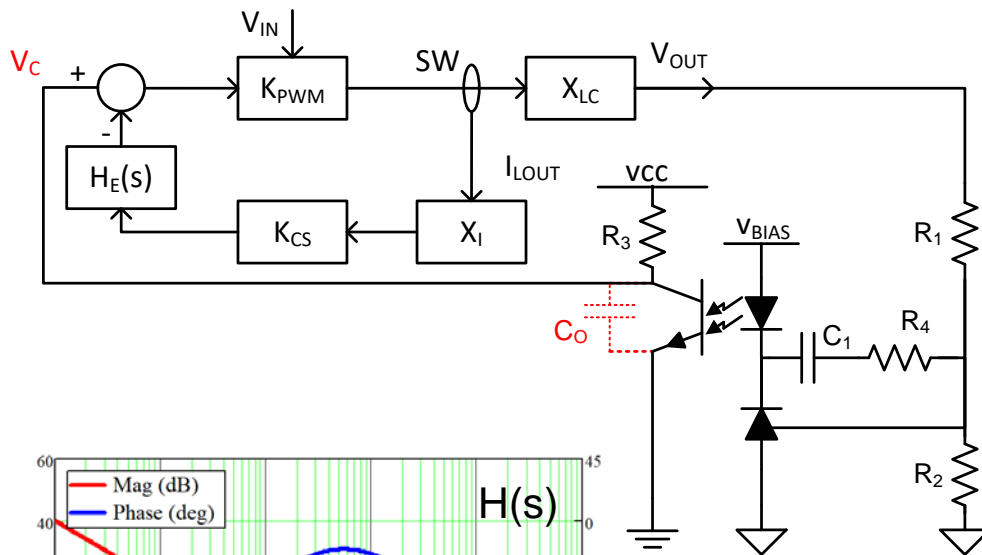
- Connect LED to a fixed bias rail.

Optocoupler CTR has a wide part to part variation and is also a function of -

- LED current,
- Temperature,
- Age.

Perceived to be unreliable, but main issue is lifetime

Very useful for crossing an isolation barrier



Pole at origin,
Zero, R_1C_1
HF pole at R_3C_0

Current Loop Stability:

Measuring gain and phase of the current loop is difficult.

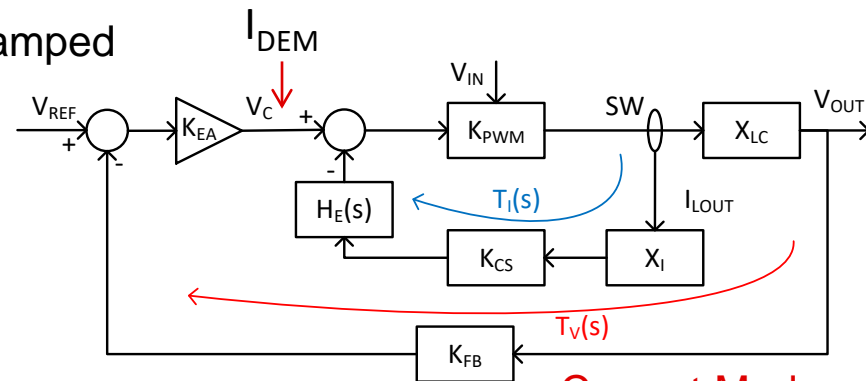
Fix an operating point (Constant I_{DEM}), inject the signal in series with the CS resistor, measure the gain and phase vs frequency

However: Current loop stability is not normally a problem except

In CCM a fixed frequency current loop is unstable for $D > 50\%$, Sub Harmonic Oscillations

Operation at D slightly below 50% can be underdamped

Slope Compensation Ramp needed



Current Mode
Control (CMC)

Ref 9



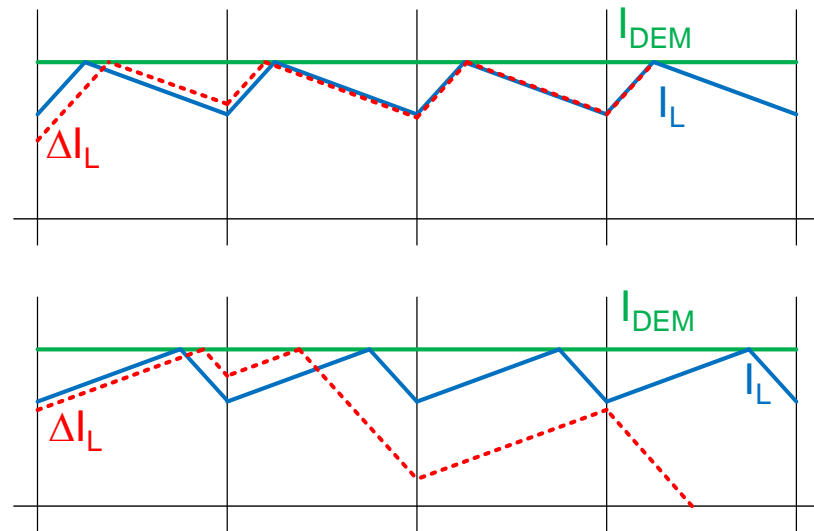
Sub-Harmonic Oscillations: Instability

$D < 50\%$, perturbation in inductor current (dotted) dies away.

System becomes increasingly underdamped as D increases past 40%

$D > 50\%$, perturbation in inductor current does not die away. Current diverges. System is unstable

Characterised by large cycle to cycle variations



Green = Current Demand Signal
Blue = steady state inductor current
Red = perturbed inductor current

Ref 7



Sub-Harmonic Oscillations: Slope Compensation

Slope Compensation Ramp stabilises the system

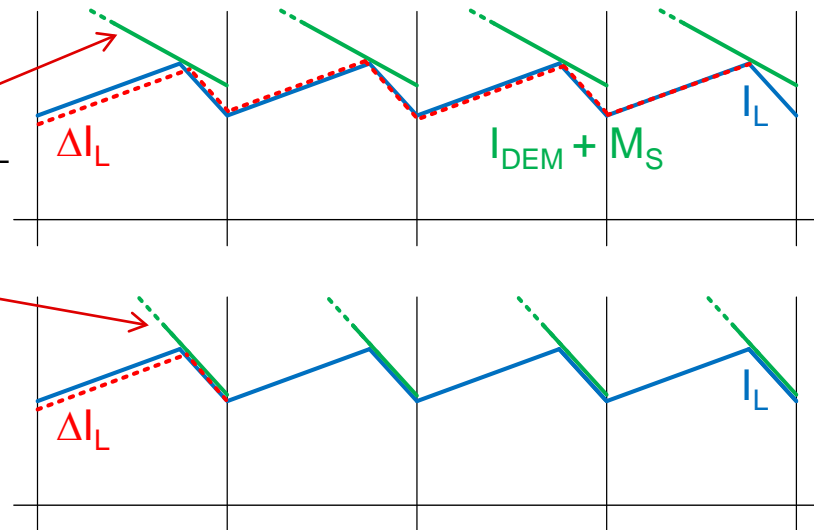
- m_S : at least 50% of inductor current downslope m_L
Min Peak to Average error when $m_S = -50\% m_L$
- Fastest recovery when $m_S = -100\% m_L$
- Non-Linear Slope Compensation is possible
– rarely used

Slope can be subtracted from I_{DEM} OR Added to the Inductor Current signal

Slope compensation should be added for $D > 40\%$

Response becomes increasingly underdamped as D approaches 50%

Ref 8



Green = Current Demand Signal
+ Slope Compensation Ramp
Blue = steady state inductor current
Red = perturbed inductor current



References

- 1/ The Right Half plane Zero, A Simplified Explanation, Dixon: <https://www.ti.com/seclit/ml/slup084/slup084.pdf>
- 2/ Fundamentals of Power Supply Design: Mammano: Texas Instruments, 2017
- 3/ SMPS compensation made easy, Sheehan: <https://www.ti.com/seclit/ml/slup340/slup340.pdf>
- 4/ Control Loop Cookbook, Dixon: <https://www.ti.com/seclit/ml/slup113/slup113.pdf>
- 5/ Compensation Design with TL431 for UCC28600: <http://www.ti.com/lit/an/slua671/.pdf>
- 6/ Designing with the TL431, Ridley: https://www.researchgate.net/publication/280308828_Designing_with_the_TL431_-_the_first_complete_analysis
- 7/ A more Accurate Current-Mode Control Model, Ridley: <https://www.ti.com/seclit/ml/slup122/slup122.pdf>
- 8/ Modelling, Analysis and Compensation of the Current Mode Converter: <http://www.ti.com/lit/an/slua101/slua101.pdf>
- 9/ Average Current Mode Control of Switching Power Supplies, Dixon: <https://www.ti.com/seclit/ml/slup091/slup091.pdf>
- 10/ Considerations for measuring loop gain in power supplies: <https://www.ti.com/seclit/ml/slup386/slup386.pdf>
- 11/ Fundamentals of Power Electronics: Erickson and Maksimovic, ISBN 0-7923-7270-0
- 12/ Modern Control Systems: Dorf, Addison Wesley, ISBN: 0-201-51713-2
- 13/ http://www.how2power.com/pdf_view.php?url=/newsletters/1204/articles/H2PToday1204_design_TexasInstruments.pdf
- 14/ <http://venable.biz/uploads/files/01-Technical-Paper-Testing-Power-Sources-for-Stability.pdf>
- 15/ https://en.wikipedia.org/wiki/Bicycle_and_motorcycle_dynamics



Control of SMPS – a Refresher

End of Part 2

Colin Gillmor (APP, HPC)

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Control of SMPS – a Refresher

Part 3

Colin Gillmor (APP, HPC)



Control of SMPS – a Refresher:

Agenda

- Part 1 {
 - 1. Concepts
 - 2. Transfer Functions
 - 3. Control Systems
 - Part 2 {
 - 4. Loop Transfer Functions
 - Control to Output: $G(s)$
 - Output to Control: $H(s)$
 - 5. Loop Compensation
 - Part 3 {
 - 6. Measuring the Control Loop
 - 7. Summary and other issues
 - 8. References
- Power Stage (Plant)
Feedback (Control)



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Feedback (Control)

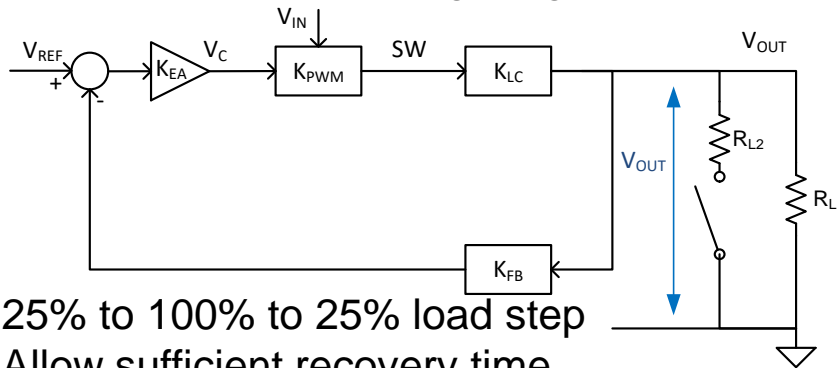




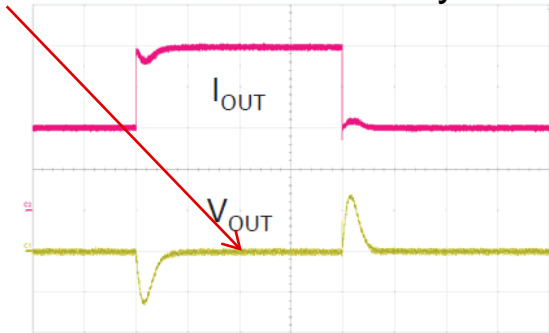
Measuring the control loop:

Transient Response

Quick, Qualitative, Large Signal

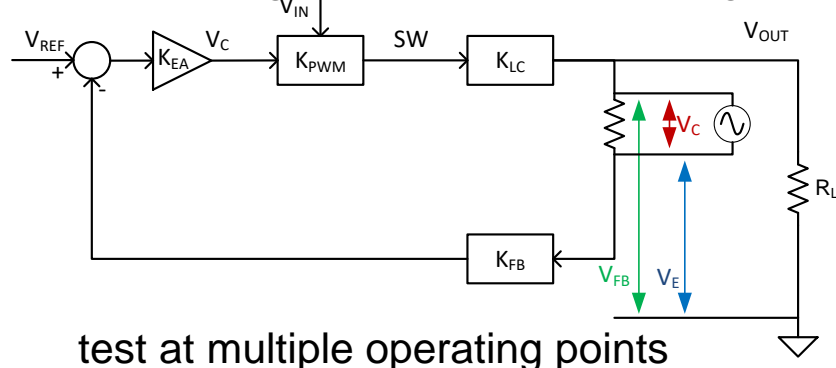


25% to 100% to 25% load step
Allow sufficient recovery time



Loop Response

Time Consuming, Quantitative, Small Signal

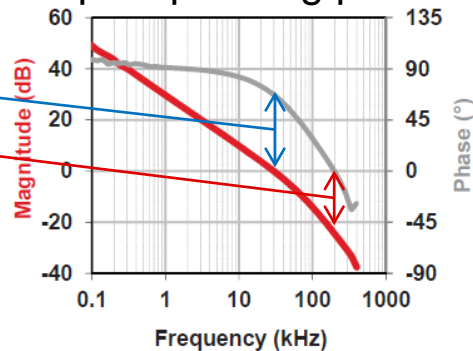


test at multiple operating points

Loop b/w 30kHz
Phase Margin $\approx 60^\circ$
Gain Margin ≈ 20 dB

Laplace Transform

Inverse Laplace Transform



Measuring the control loop: Bode Plot

Signal injection:

Isolation transformer couples test signal into circuit

- Wide bandwidth – typ 100Hz to 100kHz

Signal injection location must be chosen carefully

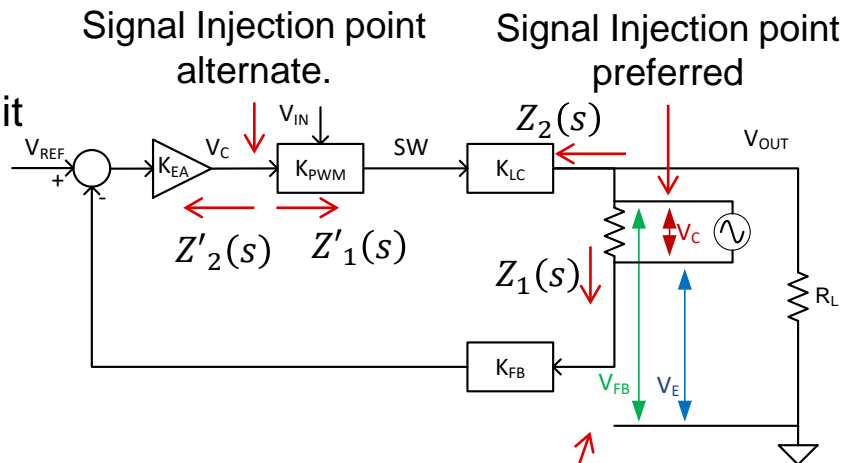
- Low Z looking 'back' into the loop, $Z_2(s)$
- High Z looking 'forward' around the loop, $Z_1(s)$

$$T(s) = M(s) * \frac{Z_1(s)}{Z_1(s) + Z_2(s)}$$

Where $T(s)$ is the true loop gain, $M(s)$ is the measured loop gain
 $Z_1(s)$ and $Z_2(s)$ are difficult to quantify but if $Z_1(s) \gg Z_2(s)$ then

$$T(s) \approx M(s)$$

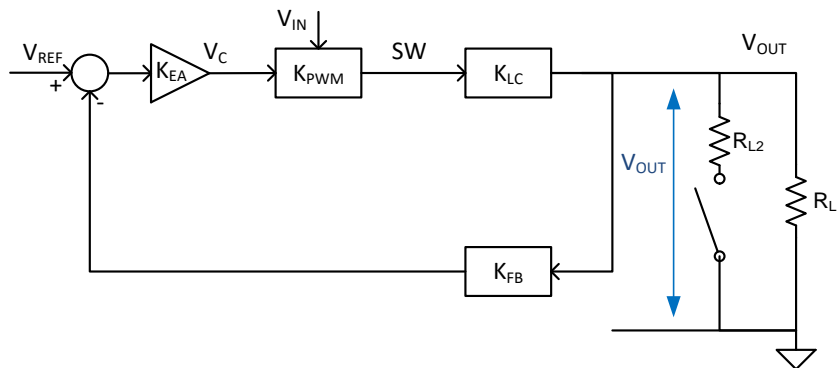
Ref 10, Ref 14



In series with K_{FB} is ideal but meters may limit use at high V_{out}

Measuring the control loop: Transient Response

Transient Response
Quick, Qualitative, Large Signal



Fourier transform of a step waveform contains components at all frequencies.

Large amplitude Load change

- Typically 25% to 75% to 25% load steps
- 0% to 100% to 0% load steps are also used
-

Load di/dt must be significantly faster than the loop response.

- Electronic Load step function
- Resistor with MOSFET switch

Signal amplitude can be 'buried' in noise

- Apply repeated transients and average the result



Measuring the control loop

Formal relationship between Gain/Phase plot and Transient Response (LTI system)

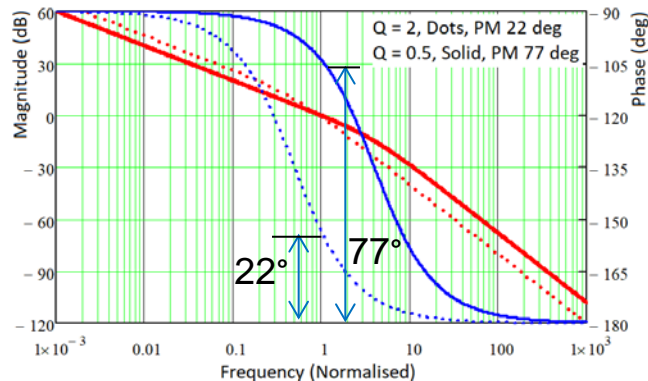
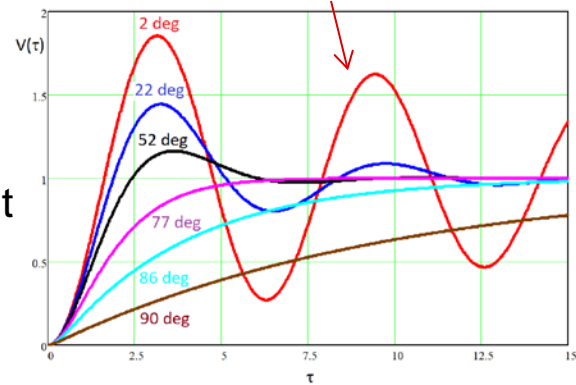
Phase Margin can be estimated from the shape of the transient response

Plots here are normalised to a crossover at 1Hz

Underdamped transient response implies small phase margin

Loop stability can be estimated from a load transient test

Oscillation at crossover frequency of the loop (approx.)



Ref 11, PP342



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The Iceberg Analogy

Most instability problems have nothing to do with classical control theory !

- Noise Pickup
- Non Linearity – insufficient control range/authority
- Over Current protections
- Input Filter Oscillations
- Problems with Remote Sensing
- Source Instability
- Load Instability
- Etc. etc
- Etc.



Control of SMPS: Summary

Control theory is sometimes thought to be difficult to understand

- Complex Mathematics, Complex Frequency, Laplace Transform, Poles, Zeros etc etc
- An intuitive overview is possible without too much complexity

SMPS control

- Voltage Mode:
- Current Mode: Peak Current Mode, Average Current Mode

Loop Transfer Functions

- Control to Output: $G(s)$, Output to Control: $H(s)$, Complete Loop
- Loop Compensation: Type 1, Type 2, Type 3

Testing

- Gain Phase Measurements (Bode Plot), Transient Tests, Evaluation of results.

References



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- 2/ Fundamentals of Power Supply Design: Mammano: Texas Instruments, 2017
- 3/ SMPS compensation made easy, Sheehan: <https://www.ti.com/seclit/ml/slup340/slup340.pdf>
- 4/ Control Loop Cookbook, Dixon: <https://www.ti.com/seclit/ml/slup113/slup113.pdf>
- 5/ Compensation Design with TL431 for UCC28600: <http://www.ti.com/lit/an/slua671/.pdf>
- 6/ Designing with the TL431, Ridley: https://www.researchgate.net/publication/280308828_Designing_with_the_TL431_-_the_first_complete_analysis
- 7/ A more Accurate Current-Mode Control Model, Ridley: <https://www.ti.com/seclit/ml/slup122/slup122.pdf>
- 8/ Modelling, Analysis and Compensation of the Current Mode Converter: <http://www.ti.com/lit/an/slua101/slua101.pdf>
- 9/ Average Current Mode Control of Switching Power Supplies, Dixon: <https://www.ti.com/seclit/ml/slup091/slup091.pdf>
- 10/ Considerations for measuring loop gain in power supplies: <https://www.ti.com/seclit/ml/slup386/slup386.pdf>
- 11/ Fundamentals of Power Electronics: Erickson and Maksimovic, ISBN 0-7923-7270-0
- 12/ Modern Control Systems: Dorf, Addison Wesley, ISBN: 0-201-51713-2
- 13/ http://www.how2power.com/pdf_view.php?url=/newsletters/1204/articles/H2PToday1204_design_TexasInstruments.pdf
- 14/ <http://venable.biz/uploads/files/01-Technical-Paper-Testing-Power-Sources-for-Stability.pdf>
- 15/ https://en.wikipedia.org/wiki/Bicycle_and_motorcycle_dynamics



Control of SMPS – a Refresher

End of Part 3

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